

## Global Optimization Initiative

Michael R. Bussieck, Alexander Meeraus GAMS Development Corporation

OR2001, Duisburg



#### Introduction

Background and Motivation

www.gamsworld.org

Global Optimization

Future



#### View Points

Research Priorities and Incentives

Numeric and Symbolic Software

User Risk

Change in User Focus

Quality Assurance

Dissemination

Market Segmentation



## Change in Focus

### Computation Past

- Algorithm limits applications
- Problem representation is low priority
- Large costly projects
- Long development times
- Centralized expert groups
- High computational cost, mainframes
- Users left out

#### **Model** Present

- Modeling skill limits applications
- Algebraic model representation
- Smaller projects
- Rapid development
- Decentralized modeling teams
- Low computational cost, workstations
- Machine independence
- Users involved

### **Application Future**

- Domain expertise limits application
- Off-the-shelf graphical user interfaces
- Links to other types of models
- Models embedded in business applications
- New computing environments
- Internet/web
- Users hardly aware of model



## GAMS World Home Page





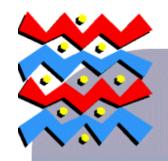
### Purpose of GAMS World

...a web site aiming to bridge the gap between academia and industry by providing highly focused forums and dissemination services in specialized areas of mathematical programming.

Substantial progress in the 1980s and 1990s .... application of these tools less than expected .... abstraction, expression, and translation of real world requires highly specialized and domains specific knowledge ... process of acquisition and dissemination of this knowledge is complex and poorly understood...process of transforming a new algorithm into a reliable and effective solution system is a slow and expensive...helping with the collection and dissemination of domain specific information and knowledge that is outside the established channels because of its content or form.



## MINLP World Home Page



#### MINLP World

**Editorial Board** 

**MINLPLib** 

**MINLP Solvers** 

MINLP List

**Related Links** 

Search

Contact

#### Welcome to the MINLP World!

MINLP World is a forum for discussion and dissemination of information about all aspects of Mixed Integer Nonlinear Programming (MINLP).

MINLP models are models that combine combinatorial aspects with nonlinearities. MINLP models are much more difficult than both Mixed Integer Linear Programming (MIP) and Nonlinear Programming (NLP) models.

MINLP is still a new field, and we cannot yet solve all the problems that naturally fall within this area. It is the purpose of this site to bring people that work with MINLP together. We are interested in practical software (MINLP Solvers), testing, comparison, and quality of solvers (MINLPLib), research in both solution methods and in good model formulations, and in improving the communication between people interested in these topics (Related Links and MINLP list).

MINLP World is featured by GAMS World



## MPEC World Home Page



Editorial Board

MPECLib

**MPEC Solvers** 

MPEC List

**Related Links** 

Search

Contact

#### **MPEC World**

#### Welcome to the MPEC World!

MPEC World is a forum for discussion and dissemination of information about all aspects of Mathematical Programs with Equilibrium Constraints (MPEC).

MPEC is a relatively new field (not nearly so mature as LP or NLP), and we cannot yet solve many of the problems that naturally fall within this area. It is the purpose of this site to bring people that work with MPEC together. We are interested in practical software (MPEC Solvers), testing, comparison, and quality of solvers (MPECLib), research in both solution methods and in good model formulations, and in improving the communication between people interested in these topics (Related Links and MPEC list).

MINLP World is featured by GAMS World



## Global World Home Page



#### **GLOBAL World**

**Editorial Board** 

**GLOBALLib** 

**GLOBAL Solvers** 

**GLOBAL List** 

Related Links

Search

Contact

#### Welcome to GLOBAL World!

The Global World is a forum for discussion and dissemination of all aspects of computational methods to find global optimal solutions to nonconvex nonlinear optimization problems.

Recently, general purpose global solution algorithms have been implemented and have matured into reliable solution systems that can be connected to modeling systems. These new developments make the application of nonlinear global optimization methods available to users outside the narrow global research community.

General purpose global nonlinear optimization is a new field and much work needs to be done to test the capabilities and robustness on real world models. We are interested in practical software (see <u>GLOBAL Solvers</u>) and an ever growing, well maintained library of academic and practical client test problems in the <u>GLOBAL Library</u>. Communication is supported by maintaining the <u>GLOBAL list</u> server and <u>related links</u>.

For other specialized topics in the are of mathematical programming consult the GAMS World.

GLOBAL World is featured by GAMS World

#### **Editorial Board**

#### Managing Editor

Alexander Meeraus, GAMS Development Corp., USA

#### Advisory Board

- Arne S. Drud, ARKI Consulting & Development, Denmark.
- Christodoulos A. Floudas, Department of Chemical Engineering, Princeton University, USA
- · Monique Guignard-Spielberg, Wharton School of the University of Pennsylvania, USA
- Josef Kallrath, BASF-AG, Germany
- Leon Lasdon, Management Science and Information Systems Department, College of Business Administration, University of Texas at Austin, USA
- János D. Pintér, Pinter Consulting Services, Canada
- Nikolaos V. Sahinidis, Department of Chemical Engineering, University of Illinois at Urbana-Champaign, USA



The solvers differ in the methods they use, in whether they find globally optimal solution with proven optimality, and in the size of models they can handle, and in the format of models they accept.

BARON. Branch-and-Reduce algorithm from N. Sahinidis, University of Illinois Urbana-Champaign

LGO. Lipschitz Global Optimization from Pinter Consulting Services, Canada

OQGRG. OptQuest/GRG algorithms by OptTek Systems and Optimal Methods

# GAMS BARON

BARON is a computational system for solving non convex optimization problems to global optimality. Purely continuous, purely integer, and mixed-integer nonlinear problems can be solved with the software. The Branch And Reduce Optimization Navigator derives its name from its combining interval analysis and duality in its reduce arsenal with enhanced branch and bound concepts as it winds its way through the hills and valleys of complex optimization problems in search of global solutions.

# GAMS

LGO combines rigorous statistical methods with traditional mathematical programming methods to find solutions within well defined bounds. Tailored versions of LGO have been applied successfully in number of large scale special purpose applications.

# GAMS OQGRG

OQGRG. This system combines the robust nonlinear optimization technology from Optimal Methods with OptTek's state-of-the-art metaheuristic search procedures, including Tabu Search, Neural Networks, and Scatter Search, into a single composite method.

GLOBALLib is a collection of Nonlinear Programming models. The purpose of the collection is to provide algorithm developer of global optimization codes with a large and varied set of both theoretical and practical test models.

- · Browse GLOBALLib by model name
- · Browse GLOBALLib by author/contributor
- Download GLOBALLib
- Read more about the organization of models and points in GLOBALLib
- GLOBALLib Changelog

#### Reference

GLOBALLib Bibliography

#### Scalar Models

The collection has initially been created by combining small-scale models from the literature with large industrial models. We invite everybody to make contributions to the collection. See the <u>contact page</u> for additional information.

Since many industrial models are based on proprietary information, the models have been translated into a scalar format in which documentation and comments have been removed, sets and set operators have been unrolled, and the original data and structure of the model have disappeared. Most industrial users will accept that translated confidential models can be made publicly available. The scalar models are not intended to serve as guidelines for good modeling practice.



## **GLOBALLib Model Statistics**

Name	Туре	#Eqns	#Vars	#NZ	#NNZ	Bestknown	at Point
abel	NLP	15	31	101	30		
alkyl	NLP	8	15	32	19	-1.7650	<u>p1</u>
bearing	NLP	13	14	41	28	1.9517	<u>p1</u>
camege	NLP	243	280	1356	850		
camens	NLP	243	280	1356	850		
camshape 100	NLP	201	200	697	299		
camshape200	NLP	401	400	1397	599		
camshape400	NLP	801	800	2797	1199		
camshape800	NLP	1601	1600	5597	2399		
catmix100	NLP	201	304	1203	1200		
catmix200	NLP	401	604	2403	2400		
catmix400	NLP	801	1204	4803	4800		
catmix800	NLP	1601	2404	9603	9600		
chain100	NLP	102	203	704	303		
chain200	NLP	202	403	1404	603		
chain400	NLP	402	803	2804	1203		
chain50	NLP	0	0	0	0		
<u>chakra</u>	NLP	42	63	143	41		
<u>chance</u>	NLP	4	5	17	4	29.8944	<u>p1</u>
<u>chem</u>	NLP	5	12	37	11		
chenery	NLP	39	44	133	56		
circle	NT.P	10	3	30	30	4 5742	n1



#### **Model Credits**

<u>Tendulkar, S</u>	<u>Tesi, A</u>	<u>Tjoa, I B</u>	Tronconi, E	Tuy, H
<u>Vanderbei, R</u>	<u>Varbrand, P</u>	Vicino, A	<u>Visweswaran, V</u>	<u>von Stryk, O</u>
Wall, TW	Westerberg, AW	Weyant, JP	Wilkinson, J H	<u>Williams, A.C.</u>
Wingo, D	Wollenberg, BF	Wood, AJ	Woolsey, R E D	Wright, MH
<u>Xue, GL</u>	Yezza, A	Zenios, S A	Zhou, S	

#### Credit List:

#### Abate, M:

- Abate, M, Barmish, B R, Murillo-Sanchez, C, and Tempo, R, Application of Some New Tools to Robust Stability Analysis of Spark Ignition Engines: A Case Study. IEEE Trans. Contr. Syst. Tech. 2 (1994), 22.
- Model:
  - o ex7 3 6

#### Ackermann, J:

- Ackermann, J, Kaesbauer, D, and Muench, R, Robust Gama-Stability Analysis in a Plant Parameter Space.
   Automatica 27 (1991), 75.
- Models:
  - o ex7 3 3
  - o ex7 3 5

## GAMS

#### Client Models

o waterz

#### GAMS Software Client Models:

- GAMS Development, GAMS Software Client Models.
- Models:
  - o 4stufen
  - o beuster
  - o deb10
  - o deb6
  - o deb7
  - o deb8
  - o deb9
  - o detf1
  - o johnall
  - o <u>saa 2</u>
  - o var con10



## Sample 'scalar' model (1)

#### alkyl.gms:

#### Reference:

- Berna, T, Locke, M, and Westerberg, A W, A New Approach to Optimization of Chemical Processes.
   American Institute of Chemical Engineers Journal 26, 1 (1980), 37-43.
- Original source: GAMS Model of <u>alkyl.gms</u> from GAMS Model Library

Point: p1

Best known point: p1 with value -1.7650

```
NLP written by GAMS Convert at 07/26/01 10:00:56
Equation counts
   Total
                                                 Х
Variable counts
                        b
                                               s2s
                                                                 вi
            cont binary integer
                                      sos1
   Total
                                              sos2
                                                               sint
                                                     scont
      15
              15
                        0
                                         0
                                                                  0
                                0
FX
       Π
               0
                        0
                                         0
                                                         0
                                                                  0
Nonzero counts
   Total
                       NL
                              DLL
           const
                       19
      32
              13
                                0
```

## GAMS

## Sample 'scalar' model (2)

```
e2.. - 0.819672131147541*x2 + x5 - 0.819672131147541*x6 =E= 0;
e3.. 0.98*x4 - x7*(0.01*x5*x10 + x4) = E = 0;
e4.. - x2*x9 + 10*x3 + x6 = E = 0;
e5.. x5*x12 - x2*(1.12 + 0.13167*x9 - 0.0067*x9*x9) =E= 0;
e6.. x8*x13 - 0.01*(1.098*x9 - 0.038*x9*x9) - 0.325*x7 =E= 0.57425;
e7.. x10*x14 + 22.2*x11 =E= 35.82;
e8.. x11*x15 - 3*x8 =E= -1.33;
* set non default bounds
x2.up = 2;
x3.up = 1.6;
x4.up = 1.2;
x5.up = 5;
x6.up = 2;
x7.10 = 0.85; x7.up = 0.93;
x8.10 = 0.9; x8.up = 0.95;
x9.10 = 3; x9.up = 12;
x10.lo = 1.2; x10.up = 4;
```

## GAMS

## Sample 'scalar' model (3)

```
x3.1 = 1.2;
x4.1 = 1.1;
x5.1 = 3.048;
x6.1 = 1.974;
x7.1 = 0.893;
x8.1 = 0.928;
x9.1 = 8;
x10.1 = 3.6;
x12.1 = 1;
x13.1 = 1;
x14.1 = 1;
x15.1 = 1;
* set non default marginals
Model m / all /;
m.limrow=0; m.limcol=0;
$if NOT '%gams.u1%' == '' $include '%gams.u1%'
Solve m using NLP minimizing objvar;
```



#### **Point Information**

#### Point p1 for model bearing.gms (Best known point)

Solution found by BARON Solution value: 1.95173322000

#### Point: pl



#### **Translation Service**

In order to use the GMS2XX translation service you have to attach your model to an email to our translation server at <a href="mailto:gms2xx@gamsworld.org">gms2xx@gamsworld.org</a>. You specify the language in the subject line, for example

Subject: GAMS

At the moment we support the following languages:

- AMPL
- BARON
- CplexLP
- CplexMPS
- GAMS
- LGO
- LINGO
- MINOPT
- ALL (this creates scalar versions of all supported languages, listed above)

The attached model has to follow some conventions:

- · The extension of the attached model is .gms
- The model is self contained, i.e. no \$include or \$batinclude
- . No execution of external programs is allowed, i.e. no \$call or execute
- . No file creation, i.e. no put files or \$echo



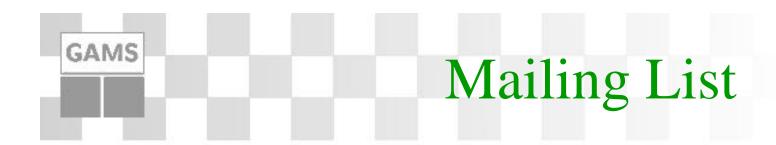
## LGO Example

```
Nonzero counts
С
      Total
              const
                         NL
                                DLL
С
         19
                 19
                          0
                                  0
С
C **** 8 bounds have been reset in file lgo.in
      Subroutine USER FCT(x,obj,objname,ctype,g,gname)
      implicit real*8 (a-h,o-z)
     DLL EXPORT USER FCT
      dimension x(7), ctype(6), g(6), gname(6)
      character*20 gname,objname
      integer*2 ctype
      objname=' '
      do i=1,6
      gname(i)=^{-1}
      end do
      q(1) = -0.225*x(1) - 0.153*x(2) - 0.162*x(3) - 0.225*x(4)
     \cdot - 0.162*x(5) - 0.126*x(6) + x(7)
     ctype(1) = 0
      g(2) = x(1) + x(2) + x(3) - 350
      ctype(2) = -1
      g(3) = x(4) + x(5) + x(6) - 600
      ctype(3) = -1
```



## Lingo Example

```
! FX
  Nonzero counts
     Total
                        NL
                               DLL
             const
                               0
        19
                19
                         0
MODEL:
[Obj] MIN = x7;
[e1] - 0.225*x1 - 0.153*x2 - 0.162*x3 - 0.225*x4 - 0.162*x5 - 0.126*x6 + x7
     = 0;
[e2]
     x1 + x2 + x3 <= 350;
[e3]
     X4 + x5 + x6 <= 600;
      x1 + x4 >= 325;
[e4]
     x2 + x5 >= 300;
[e5]
     x3 + x6 >= 275;
[e6]
@Free(x7);
End
Init:
End
```



We set up a mailling list for exchanging all sorts of materials, problems, and questions concerning GLOBAL optimization problems.

To **subscribe** to the list send a message to <u>global-1-request@gamsworld.org</u> containing the word *subscribe* only in the subject line.

To post to the list after you subscribed send your mail to global-l@gamsworld.org.

You can **unsubscribe** anytime in a similar way: send a message to <u>global-1-request@gamsworld.org</u> containing the word *unsubscribe* only in the subject line.

To obtain more information about your options concerning the list, send a message to the list server account <a href="mailto:listar@gamsworld.org">listar@gamsworld.org</a> containing the word <a href="mailto:help">help</a> only in the subject line.

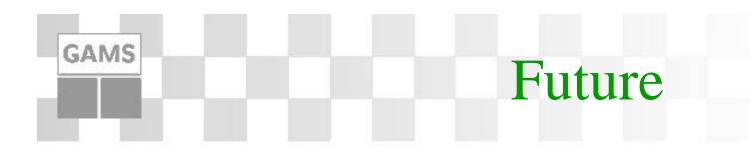


## globallib.gms

The library also contains the GAMS model globallib.gms that helps organizing the models and points in the GLOBALLib. All models are matched with propper references to contributors, publications, and application areas.

The model also help to create batch execution scripts. For example, the following piece of GAMS code creates a batch script that runs models that come from the book "Handbook of Test Problems in Local and Global Optimization" by Floudas e.a. with solver OQGRG:

```
file frs batch run script / rs.bat /;
loop(m$mr(m,"r1"),
  put frs "gams " m.tl:0 " nlp=oqgrg dnlp=oqgrg cns=oqgrg " /;
);
```



Expand GAMSWORLD Coverage

More Source to Source Translations

Preprocessing and Reformulation

**Developer Tools** 

**QA** Tools