

# Results

June 18, 2010

## 1 Tables of Friedman, Aligned Friedman, Bonferroni-Dunn, Holm, Hochberg and Hommel Tests

Table 1: Average Rankings of the algorithms (Friedman)

| Algorithm | Ranking            |
|-----------|--------------------|
| DE        | 2.6578947368421058 |
| CHC       | 0.9999999999999996 |
| VXQR1     | 2.342105263157894  |

Friedman statistic (distributed according to chi-square with 2 degrees of freedom: 29.44736842105258. P-value computed by Friedman Test: 4.03277710669947E-7.

Iman and Davenport statistic (distributed according to F-distribution with 2 and 36 degrees of freedom: 61.975384615384144. P-value computed by Iman and Davenport Test: 2.1962967524993484E-12.

Table 2: Average Rankings of the algorithms (Aligned Friedman)

| Algorithm | Ranking            |
|-----------|--------------------|
| DE        | 35.763157894736835 |
| CHC       | 11.31578947368421  |
| VXQR1     | 39.92105263157895  |

Aligned Friedman statistic (distributed according to chi-square with 2 degrees of freedom: 12.953645011035965. P-value computed by Aligned Friedman Test: 0.0015386921215805316.

Table 3: Average Rankings of the algorithms (Quade)

| Algorithm | Ranking             |
|-----------|---------------------|
| DE        | 2.55000000000000003 |
| CHC       | 1.0                 |
| VXQR1     | 2.44999999999999997 |

Quade statistic (distributed according to F-distribution with 2 and 36 degrees of freedom: 24.73972602739726. P-value computed by Quade Test: 1.7375362808383028E-7.

Table 4: Contrast Estimation

|       | DE     | CHC   | VXQR1 |
|-------|--------|-------|-------|
| DE    | 0.000  | -1899 | 178.8 |
| CHC   | 1899   | 0.000 | 2078  |
| VXQR1 | -178.8 | -2078 | 0.000 |

Table 5: Holm / Hochberg / Holland / Rom / Finner / Li Table for  $\alpha = 0.05$  (FRIEDMAN)

| $i$ | algorithm | $z = (R_0 - R_i)/SE$ | $p$                  | Holm/Hochberg/Hommel | Holland              | Rom   | Finner               | Li                  |
|-----|-----------|----------------------|----------------------|----------------------|----------------------|-------|----------------------|---------------------|
| 2   | DE        | 5.109974765619023    | 3.222018441378448E-7 | 0.025                | 0.025320565519103666 | 0.025 | 0.025320565519103666 | 0.05262972411163838 |
| 1   | VXQR1     | 4.136646238834443    | 3.524187887096871E-5 | 0.05                 | 0.050000000000000044 | 0.05  | 0.050000000000000044 | 0.05                |

Bonferroni-Dunn's procedure rejects those hypotheses that have a p-value  $\leq 0.025$ .

Hochberg's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Hommel's procedure rejects all hypotheses.

Rom's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Li's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Table 6: Holm / Hochberg / Holland / Rom / Finner / Li Table for  $\alpha = 0.05$  (ALIGNED FRIEDMAN)

| $i$ | algorithm | $z = (R_0 - R_i) / SE$ | $p$                   | Holm/Hochberg/Hommel | Holland              | Rom   | Finner               | Li                  |
|-----|-----------|------------------------|-----------------------|----------------------|----------------------|-------|----------------------|---------------------|
| 2   | VXQR1     | 5.311864015748826      | 1.0850956297527696E-7 | 0.025                | 0.025320565519103666 | 0.025 | 0.025320565519103666 | 0.05263128253858566 |
| 1   | DE        | 4.539762346486346      | 5.631766872610135E-6  | 0.05                 | 0.050000000000000044 | 0.05  | 0.050000000000000044 | 0.05                |

Bonferroni-Dunn's procedure rejects those hypotheses that have a p-value  $\leq 0.025$ .

Hochberg's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Hommel's procedure rejects all hypotheses.

Rom's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Li's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Table 7: Holm / Hochberg / Holland / Rom / Finner / Li Table for  $\alpha = 0.05$  (QUADE)

| $i$ | algorithm | $z = (R_0 - R_t)/SE$ | $p$                  | Holm/Hochberg/Hommel | Holland              | Rom   | Finner               | Li                   |
|-----|-----------|----------------------|----------------------|----------------------|----------------------|-------|----------------------|----------------------|
| 2   | DE        | 4.190075270115177    | 2.788619345680359E-5 | 0.025                | 0.025320565519103666 | 0.025 | 0.025320565519103666 | 0.052626913596485914 |
| 1   | VXQR1     | 3.919747833333551    | 8.864166676775197E-5 | 0.05                 | 0.050000000000000044 | 0.05  | 0.050000000000000044 | 0.05                 |

Bonferroni-Dunn's procedure rejects those hypotheses that have a p-value  $\leq 0.025$ .

Hochberg's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Hommel's procedure rejects all hypotheses.

Rom's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Li's procedure rejects those hypotheses that have a p-value  $\leq 0.05$ .

Table 8: Adjusted  $p$ -values (FRIEDMAN)

| $i$ | algorithm | unadjusted $p$       | $p_{Bonf}$           | $p_{Holm}$           | $p_{Hoch}$           | $p_{Hommel}$         |
|-----|-----------|----------------------|----------------------|----------------------|----------------------|----------------------|
| 1   | DE        | 3.222018441378448E-7 | 6.444036882756896E-7 | 6.444036882756896E-7 | 6.444036882756896E-7 | 6.444036882756896E-7 |
| 2   | VXQR1     | 3.524187887096871E-5 | 7.048375774193742E-5 | 3.524187887096871E-5 | 3.524187887096871E-5 | 3.524187887096871E-5 |

Table 9: Adjusted  $p$ -values (FRIEDMAN)

| $i$ | algorithm | unadjusted $p$       | $p_{Holl}$           | $p_{Rom}$            | $p_{Finn}$           | $p_{Li}$              |
|-----|-----------|----------------------|----------------------|----------------------|----------------------|-----------------------|
| 1   | DE        | 3.222018441378448E-7 | 6.444035843822249E-7 | 6.444036882756896E-7 | 6.444035843822249E-7 | 3.2221309571508097E-7 |
| 2   | VXQR1     | 3.524187887096871E-5 | 3.524187887093966E-5 | 3.524187887096871E-5 | 3.524187887093966E-5 | 3.524187887096871E-5  |



Table 10: Adjusted  $p$ -values (ALIGNED FRIEDMAN)

| $i$ | algorithm | unadjusted $p$        | $p_{Bonf}$             | $p_{Holm}$            | $p_{Hoch}$            | $p_{Hommel}$          |
|-----|-----------|-----------------------|------------------------|-----------------------|-----------------------|-----------------------|
| 1   | VXQR1     | 1.0850956297527696E-7 | 2.17019112595055392E-7 | 2.1701912595055392E-7 | 2.1701912595055392E-7 | 2.1701912595055392E-7 |
| 2   | DE        | 5.631766872610135E-6  | 1.126353374522027E-5   | 5.631766872610135E-6  | 5.631766872610135E-6  | 5.631766872610135E-6  |

Table 11: Adjusted  $p$ -values (ALIGNED FRIEDMAN)

| $i$ | algorithm | unadjusted $p$        | $p_{Holl}$            | $p_{Rom}$             | $p_{Finn}$            | $p_{Li}$              |
|-----|-----------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| 1   | VXQR1     | 1.0850956297527696E-7 | 2.1701911423477327E-7 | 2.1701912595055392E-7 | 2.1701911423477327E-7 | 1.0851016230482409E-7 |
| 2   | DE        | 5.631766872610135E-6  | 5.631766872626898E-6  | 5.631766872610135E-6  | 5.631766872626898E-6  | 5.631766872610135E-6  |

Table 12: Adjusted  $p$ -values (QUADE)

| $i$ | algorithm | unadjusted $p$       | $p_{Bonf}$           | $p_{Holm}$           | $p_{Hoch}$           | $p_{Hommel}$         |
|-----|-----------|----------------------|----------------------|----------------------|----------------------|----------------------|
| 1   | DE        | 2.788619345680359E-5 | 5.577238691360718E-5 | 5.577238691360718E-5 | 5.577238691360718E-5 | 5.577238691360718E-5 |
| 2   | VXQR1     | 8.864166676775197E-5 | 1.772833333550393E-4 | 8.864166676775197E-5 | 8.864166676775197E-5 | 8.864166676775197E-5 |

Table 13: Adjusted  $p$ -values (QUADE)

| $i$ | algorithm | unadjusted $p$       | $p_{Hol}$             | $p_{Rom}$            | $p_{Finn}$            | $p_{Li}$              |
|-----|-----------|----------------------|-----------------------|----------------------|-----------------------|-----------------------|
| 1   | DE        | 2.788619345680359E-5 | 5.5771609273946865E-5 | 5.577238691360718E-5 | 5.5771609273946865E-5 | 2.7887887798626436E-5 |
| 2   | VXQR1     | 8.864166676775197E-5 | 8.864166676769702E-5  | 8.864166676775197E-5 | 8.864166676769702E-5  | 8.864166676775197E-5  |